

## Self-Assembly of Flexible Linear–Semiflexible Bottlebrush–Flexible Linear Triblock Copolymers

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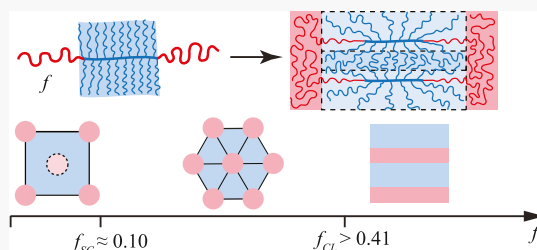
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**ABSTRACT:** Block copolymer (BCP) self-assembly is a fundamental process in which incompatible blocks spontaneously form organized microstructures with broad practical applications. Classical understanding is that the domain spacing is limited by the contour length of the polymer backbone. Here, using a combination of molecular design, chemical synthesis, small-/wide-angle X-ray scattering, transmission electron microscopy, and electron tomography, we discover that this molecular picture does not hold for architecturally semiflexible BCPs. For strongly segregated linear–semiflexible bottlebrush–linear triblock copolymers, the size of the bottlebrush domain can be twice the bottlebrush backbone contour length.

The mechanism of such anomalous self-assembly is likely that the interfacial repulsion between the incompatible blocks is large enough to pull a part of the linear end blocks into the bottlebrush domain. This effectively increases the bottlebrush domain size. Moreover, the semiflexible bottlebrush widens the regime for the cylinder morphology that is associated with the volume fraction of the end blocks  $f_C^{\text{SFB}} \in (0.10, >0.41)$ . This window is much wider than that for flexible linear BCPs,  $f_C^{\text{F}} \in (0.14, 0.35)$ , and that predicted by the recent self-consistent field theory for linear-bottlebrush BCPs of the same chemistry and molecular architecture. Our experimental findings reveal previously unrecognized mechanisms for the self-assembly of architecturally complex BCPs.



### INTRODUCTION

A block copolymer (BCP) consists of two or more chemically distinct polymeric blocks linked by covalent bonds. BCP self-assembly is a fundamental process in which the incompatible blocks spontaneously form organized microstructures, which have broad applications in many technologically important areas;<sup>1,2</sup> examples include thermoplastic elastomers,<sup>3</sup> templates for lithography,<sup>4</sup> porous structures for filtration and separation,<sup>5,6</sup> and drug carriers.<sup>7</sup> Critical to these diverse applications is a wide range of macroscopic properties, which are largely determined by the type and the characteristic length of the self-assembled microstructures. The characteristic length scale afforded by classical flexible linear BCPs is intrinsically small, however. It is largely determined by the molecular weight (MW) of polymers and is often below  $\sim 100$  nm.<sup>8</sup> Further increasing the MW inevitably forms entanglements,<sup>9</sup> which slow down polymer dynamics and thus lead to uncontrollable self-assembly.<sup>4</sup> This limitation can be circumvented using bottlebrush-based BCPs,<sup>6</sup> in which at least one block is a bottlebrush polymer with a linear backbone densely grafted by many side chains.<sup>10</sup> This strategy has been exploited to create photonic crystals with characteristic lengths comparable to visible light,<sup>11</sup> solvent-free polymer networks of extreme softness<sup>12,45</sup> mimicking “watery” biological tissue,<sup>14</sup> elastomers with an exceptional combination of softness and structural coloration,<sup>15</sup> and, very recently, a reprocessable soft elastomer

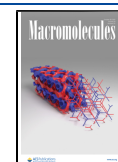
for additive manufacturing.<sup>16</sup> These properties and applications highlight the potential of bottlebrush-based BCPs as an emerging platform for material design and innovation.

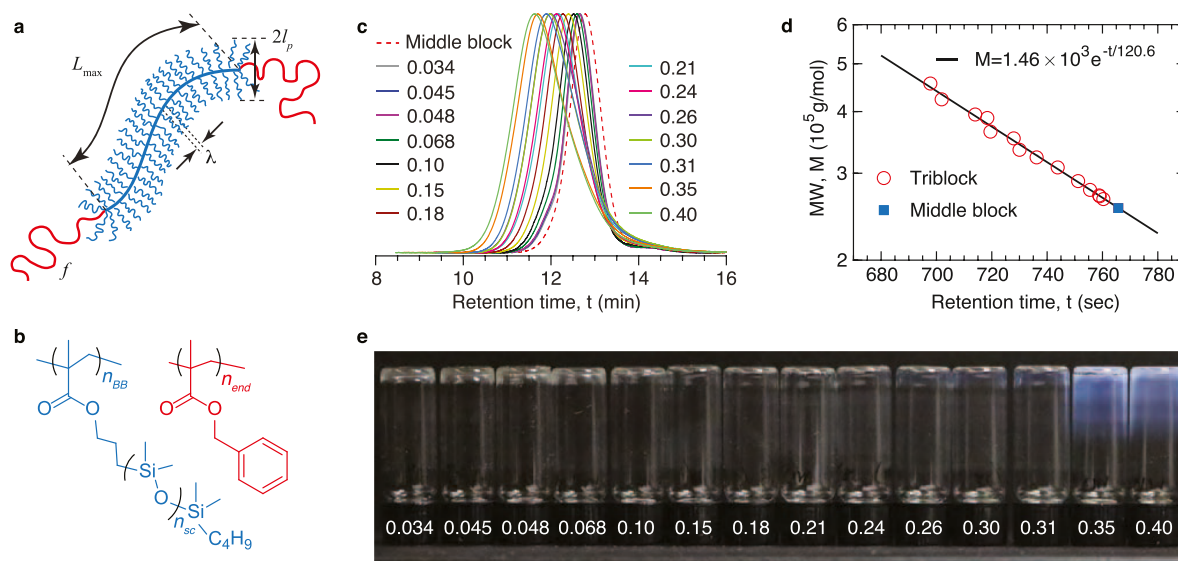
Unlike a linear polymer whose flexibility is constant, a bottlebrush can be physically flexible, semiflexible, or rigid. For example, increasing the size and/or grafting density of side chains stiffens the bottlebrush polymer.<sup>10</sup> To minimize excluded volume interactions, stiff polymers are prone to form highly ordered structures, a phenomenon often seen in liquid crystals<sup>17</sup> and in rod-coil BCPs.<sup>18,19</sup> However, this understanding does not apply to bottlebrush-based BCPs. For instance, recently, we experimentally discovered that at small volume fractions of end blocks,  $f < 0.05$ , linear–bottlebrush–linear (LBBL) triblock copolymers self-assemble into spherical microstructures regardless of the bottlebrush flexibility.<sup>45</sup> These findings were confirmed by the self-consistent field theory (SCFT) for the self-assembly of bottlebrush BCPs.<sup>20</sup> Moreover, although the bottlebrush as a whole is geometrically bulky, its linear side chains can rearrange to adapt to curved

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**Figure 1.** Molecular design and synthesis of flexible–semiflexible bottlebrush–flexible (F-SFB-F) triblock copolymers. (a) Schematic of a F-SFB-F triblock copolymer. The flexibility of a bottlebrush polymer is defined as  $\kappa \equiv \mathcal{L}_{\max}/2l_p$ , in which  $l_p$  (eq 1) and  $\mathcal{L}_{\max}$  (eq 2) are, respectively, the persistence length and the contour length of the bottlebrush. For a SFB,  $\kappa \approx 1$ .  $\lambda$  is the distance between two neighboring grafted side chains and  $f$  is the volume fraction of the end linear blocks. (b) In our model system, the side chain of the middle bottlebrush block is linear polydimethylsiloxane (PDMS) with a MW of 5000 g/mol, whereas the end blocks are linear poly(benzyl methacrylate) (PBnMA). The number of side chains per bottlebrush is fixed at  $n_{\text{BB}} = 51$ , whereas the number of repeating units  $n_{\text{end}}$  of the end linear blocks is increased from 31 to 570. This results in triblock copolymers that have the same SFB middle block of contour length  $\mathcal{L}_{\max} = 12.8$  nm and persistence length  $l_p \approx 5.8$  nm, whereas the mass fraction  $f_m$  of end blocks increases from 0.041 to 0.44. The corresponding volume fraction ranges from 0.034 to 0.40 based on the relation  $f = f_m/[f_m + (1 - f_m)(\rho_{\text{PBnMA}}/\rho_{\text{PDMS}})]$ , in which  $\rho_{\text{PBnMA}} = 1.18$  g/cm<sup>3</sup> and  $\rho_{\text{PDMS}} = 0.98$  g/cm<sup>3</sup> are, respectively, the densities of PBnMA and PDMS. (c) GPC traces of the bottlebrush PDMS middle block (dashed line) and all F-SFB-F triblock copolymers (solid lines). (d) The logarithmic molecular weight,  $M$ , of all triblock copolymers decreases linearly with the increase of peak retention time,  $t$ :  $M = 1.43 \times 10^8$  g/mol  $\exp(-t/120.6 \text{ sec})$ . (e) At room temperature, the polymers are optically transparent solids at  $f < 0.26$  but gradually become blue at  $f \geq 0.26$ , and the blue color becomes brighter and more obvious at  $f \geq 0.35$ .

interfaces to alleviate packing frustrations, as demonstrated by emulsions<sup>21</sup> and micelles<sup>22</sup> stabilized by bottlebrush-like surfactant molecules. These geometric and physical complexities offer a large parameter space for material design but also pose challenges in understanding the self-assembly of bottlebrush-based BCPs. Consequently, despite its fundamental and technological importance, the understanding of how the bottlebrush molecular architecture determines BCP self-assembly is far from complete.

Here, we systematically investigate the effects of composition on the self-assembly of LBBL triblock copolymers. We focus on an architecturally semiflexible bottlebrush (SFB) that dramatically differs from its flexible linear counterpart in geometrical bulkiness and physical flexibility. Using a combination of molecular design, polymer synthesis, dark-field transmission electron microscopy (TEM), electron tomography, and small-/wide-angle X-ray scattering (SAXS/WAXS), we establish the phase diagram for strongly segregated linear–semiflexible bottlebrush–linear triblock copolymers. The window for the cylinder morphology,  $f_{\text{C}}^{\text{SFB}} \in (0.10, >0.41)$ , is much wider than that for flexible linear BCPs,  $f_{\text{C}}^{\text{F}} \in (0.14, 0.35)$ , and that predicted by recent SCFT for bottlebrush-based BCPs of the same molecular architecture.<sup>20</sup> Remarkably, regardless of the type of microstructure, the size of the bottlebrush domain is always larger than the contour length of the bottlebrush backbone. Even more surprisingly, the ratio between the two length scales becomes abnormally large around 2 at high volume fractions, and this observation is reproducible. We propose that the mechanism of such

anomalous self-assembly is likely that a part of the linear end blocks is pulled into the bottlebrush domain. This provides additional space for the side chains of the bottlebrush to rearrange and effectively increases the bottlebrush domain size. These results provide qualitatively new insights into the self-assembly of architecturally complex BCPs.

## RESULTS AND DISCUSSION

**Molecular Design and Synthesis.** The flexibility  $\kappa$  of a polymer is defined as the ratio of its contour length  $\mathcal{L}_{\max}$  to twice the persistence length  $l_p$ ,  $\kappa \equiv \mathcal{L}_{\max}/(2l_p)$ , and for a semiflexible polymer,  $\kappa \approx 1$ . To design a SFB, we start with determining the dependencies of  $l_p$  and  $\mathcal{L}_{\max}$  on the bottlebrush molecular architecture (Figure 1a). In a bottlebrush, the side chains are densely grafted to a backbone polymer, occupying a cylindrical space surrounding the backbone. The cross section of the cylinder is about the size,  $R_{\text{sc}}$ , of a side chain. Within such a cylindrical space, a side chain occupies a volume,  $R_{\text{sc}}^2\lambda$ , that is the product of the cross-sectional area,  $R_{\text{sc}}^2$ , and the distance between two neighboring grafting sites,  $\lambda$ . Because of mass conservation, this volume is equal to the volume of a side chain itself,  $N_{\text{sc}}v_0$ , in which  $N_{\text{sc}}$  is the number of Kuhn monomers per side chain and  $v_0$  is the volume of a Kuhn monomer. Therefore, the cross section of the bottlebrush is  $R_{\text{sc}} \approx (N_{\text{sc}}v_0/\lambda)^{1/2}$ . The persistence length of the bottlebrush polymer is about its cross-sectional size

$$l_p \approx R_{\text{sc}} \approx (N_{\text{sc}}v_0/\lambda)^{1/2} \quad (1)$$

Table 1. Molecular Parameters of F-SFB-F Triblock Polymers<sup>a</sup>

batch	sample	microstructure											
		middle block			triblock			$q^*$ (nm <sup>-1</sup> )			$d^*$ (nm)		type
		$M_{sc}$ (kDa)	$n_{BB}$	PDI	$n_{end}$	$f$	PDI	peak	upper	lower	peak	TEM	
1	S <sub>1</sub>	5	51	1.15	31	0.034	1.17	0.3105	0.379	0.242	20.6	NA	BCC S
	S <sub>2</sub>				41	0.045	1.17	0.310	0.364	0.256	20.8	NA	BCC S
	S <sub>3</sub>				44	0.048	1.17	0.306	0.364	0.248	22.0	10.3 ± 1.4	BCC S
	S <sub>4</sub>				64	0.068	1.18	0.2615	0.302	0.221	25.5	10.4 ± 1.3	S–C
	S <sub>5</sub>				97	0.10	1.20	0.244	0.286	0.218	25.7	10.2 ± 1.3	S–C
	S <sub>6</sub>				151	0.15	1.31	0.198	0.243	0.178	31.7	16.9 ± 1.9	Hex C
	S <sub>7</sub>				193	0.18	1.36	0.181	0.217	0.157	34.7	21.0 ± 1.6	Hex C
	S <sub>8</sub>				226	0.21	1.54	0.165	0.196	0.148	38.1	NA	Hex C
	S <sub>9</sub>				278	0.24	1.55	0.159	0.194	0.136	39.5	22.6 ± 2.4	Hex C
	S <sub>10</sub>				310	0.26	1.57	0.132	0.159	0.113	47.6	NA	Hex C
	S <sub>11</sub>				378	0.30	1.60	0.128	0.158	0.111	49.1	NA	Hex C
	S <sub>12</sub>				396	0.31	1.64	0.122	0.152	0.105	51.5	NA	Hex C
	S <sub>13</sub>				478	0.35	1.71	0.0994	0.1214	0.0855	63.2	45.4 ± 5.4	Hex C
	S <sub>14</sub>				570	0.40	1.71	0.0911	0.113	0.072	68.9	53.8 ± 9.2	Hex C
2	S <sub>15</sub>			1.18	80	0.084	1.38	0.241	0.278	0.211	26.1	NA	S–C
	S <sub>16</sub>				371	0.30	1.57	0.131	0.164	0.114	47.9	NA	Hex C
3	S <sub>17</sub>			1.20	186	0.18	1.58	0.174	0.204	0.152	36.1	NA	Hex C
	S <sub>18</sub>				275	0.24	1.60	0.156	0.188	0.128	40.3	NA	Hex C
4	S <sub>19</sub>			1.17	48	0.052	1.20	0.299	0.368	0.263	21.0	NA	BCC S
	S <sub>20</sub>				124	0.12	1.26	0.218	0.259	0.192	28.8	12.6 ± 1.1	Hex C
	S <sub>21</sub>				436	0.33	1.54	0.114	0.134	0.101	55.1	NA	Hex C
5	S <sub>22</sub>			1.16	65	0.069	1.30	0.271	0.315	0.252	23.2	NA	S–C
	S <sub>23</sub>				600	0.41	1.71	0.0904	0.114	0.0691	69.5	NA	Hex C
	bbPDMS	5	51	1.15	NA	NA	NA	0.964	1.070	0.858	6.5	NA	NA

<sup>a</sup> $M_{sc}$ , molecular weight of side chains;  $n_{BB}$ , number of side chains per bottlebrush;  $n_{end}$ , number of chemical repeating units for each end linear PBnMA blocks;  $f$ , volume fraction of the end blocks; PDI, polydispersity index;  $q^*$ , wavenumber of the primary scattering peak;  $d^* = 2\pi/q^*$ , characteristic length associated with the primary scattering peak;  $D$ , domain diameter directly measured from TEM images; BCC S, body-centered cubic sphere; Hex C, hexagonal cylinder; S–C, crossover between the sphere and the cylinder; and NA, not applicable.

which increases with the side chain MW by a power of 1/2. This physical picture was described in our previous work<sup>12</sup> and others.<sup>10,23</sup> By contrast, the contour length of the bottlebrush is independent of the side chain MW; rather, it is proportional to the number of side chains per bottlebrush  $n_{BB}$

$$\mathcal{L}_{max} = n_{BB}\lambda \quad (2)$$

The bottlebrush is essentially a “fat” linear polymer, whose end-to-end distance  $R$  is described by the worm-like chain model:<sup>9</sup>  $R^2 = 2l_p\mathcal{L}_{max} - 2l_p^2\left(1 - \exp\left(-\frac{\mathcal{L}_{max}}{l_p}\right)\right)$ . The above-mentioned scaling arguments omit prefactors on the order of unity as confirmed by the molecular dynamics simulations of bottlebrush molecules.<sup>10</sup>

In our model system, the bottlebrush is formed by polymerizing methacrylate-terminated PDMS (MA-PDMS) macromonomers with a MW of 5 kg/mol (Figure 1b). This results in a bottlebrush of a grafting distance  $\lambda = 0.25$  nm. For a PDMS Kuhn monomer, the mass is  $M_0 = 381$  g/mol, the length is  $b = 1.3$  nm, and the volume is  $v_0 = 6.50 \times 10^{-1}$  nm<sup>3</sup>. Using eq 1, one obtains  $l_p \approx 5.8$  nm. Therefore, it requires about  $n_{BB} \approx 50$  side chains (eq 2) to create a SFB with  $\kappa \approx 1$ .

Guided by this molecular design, we extend our previously developed procedure<sup>16</sup> to synthesize F-SFB-F triblock copolymers (Experimental Section). The method is based on the activator-regenerated-by-electron-transfer atom transfer radical polymerization (ARGET-ATRP)<sup>24</sup> and consists of two steps: first, the synthesis of the middle bottlebrush block

and then, the two end linear blocks (Figure S1). In Step I, we use a bifunctional initiator, ethylene bis(2-bromoisobutyrate), to initiate the polymerization of the MA-PDMS macromonomer. We closely monitor the reaction and stop the polymerization at a relatively low conversion of 20%, up to which the conversion exhibits a linear dependence on the reaction time (Figure S2). This allows us to obtain a bottlebrush with precisely 51 side chains, which is determined based on the conversion of MA-PDMS macromonomers into a bottlebrush PDMS, as quantified by both proton nuclear magnetic resonance (<sup>1</sup>H NMR) spectroscopy (see Supporting Information, NMR spectra) and gel permeation chromatography (GPC) (Figure S3). Importantly, GPC reveals a narrowly distributed and symmetric retention profile with a small polydispersity index (PDI) equal to 1.15 (dashed line in Figure 1c). These results demonstrate the controlled synthesis of a semiflexible PDMS bottlebrush.

In Step II, we use the bottlebrush as a difunctional macroinitiator to grow a linear PBnMA to create triblock copolymers. For all polymers, we quantify the average MW of end blocks based on the conversion of BnMA monomers into PBnMA polymers, as determined by <sup>1</sup>H NMR (see Supporting Information NMR spectra). The purified triblock copolymers are characterized using GPC (solid lines in Figure 1c), based on which the PDI for all samples are determined (Table 1). As expected, the peak retention time decreases as the MW of the end blocks increases. Moreover, the MW determined from NMR decreases logarithmically with the increase of retention time (Figure 1d). These results confirm the accuracy of MW of

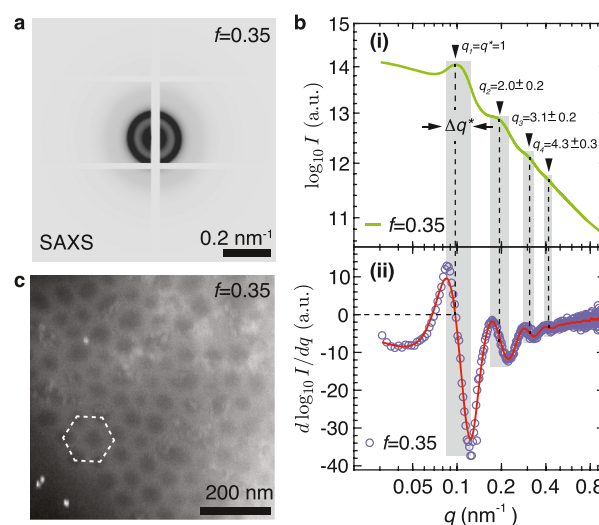
end blocks determined by NMR. Using the two-step synthesis, we obtain a series of PBnMA-bbPDMS-PBnMA triblock copolymers with the volume fraction  $f$  of the end blocks ranging from 0.034 to 0.40. Importantly, all the triblock copolymers have the same SFB middle block with  $L_{\text{max}} \approx 13$  nm and  $l_p \approx 5.8$  nm and only differ in the volume fraction of the end blocks. These polymers provide an ideal system for studying the self-assembly of F-SFB-F triblock copolymers.

At room temperature, all triblock copolymers are colorless except for those with high volume fractions,  $f \geq 0.35$ , which exhibit a light blue color (Figure 1e). This indicates ordered microstructures with characteristic lengths on the order of  $\lambda/2n \approx 120$  nm, in which  $\lambda = 380$  nm is the wavelength of blue light and  $n \approx 1.5$  is the refractive index of the polymers.<sup>8,25–27</sup> This length scale is nearly 10 times of the 13 nm contour length of the SFB backbone. Nevertheless, the transition from colorless to light blue indicates changes in the microstructure as the volume fraction increases.

**Determination of the Type of Microstructure.** The self-assembly of BCPs is driven by the minimization of free energy.<sup>28</sup> As the molecular architecture becomes more complex, however, the process toward equilibrium can be trapped in metastable states.<sup>4</sup> Also, the probability of doing so becomes high for strongly segregated BCPs<sup>29</sup> like our system with a segregation strength  $\chi N > 150$ . Here, the Flory–Huggins interaction parameter  $\chi$  between PBnMA and PDMS is about 0.26, the number of Kuhn monomers per triblock copolymer  $N$  is greater than 650, and the effects of the molecular architecture on the segregation strength are ignored. To this end, we use solvothermal annealing, a two-stage process consisting of a solvent vapor exposure, followed by thermal annealing (Experimental Section). During this process, the solvent molecules act as plasticizers and promote the mobility of individual polymer chains to achieve a thermodynamic equilibrium morphology.<sup>30–32</sup>

We use the synchrotron source to perform SAXS/WAXS measurements to characterize the microstructure for the annealed polymers (Experimental Section). In a typical measurement, an annealed polymer of cuboid shape with dimensions no smaller than  $5 \times 5 \times 1$  mm is mounted on a glass cover slip. Because the area of the sample is much larger than the beam size  $250 \mu\text{m} \times 20 \mu\text{m}$ , we perform measurements at multiple locations to ensure the consistency of the two-dimensional (2D) SAXS patterns. An example scattering pattern of the polymer with  $f = 0.35$  is shown in Figure 2a. By subtracting the background from the cover slip and radially averaging the 2D pattern, we obtain the one-dimensional (1D) scattering intensity profile as a function of the magnitude of scattering wavevector  $q$ , as shown in Figure 2b.

Next, we quantify the wavenumbers of all characteristic peaks. The primary peak is relatively sharp, exhibiting a local maximum that can be easily determined, as denoted by the first left arrow in Figure 2b(i). However, higher-order peaks are relatively broad; this makes it difficult to precisely determine their positions. Nevertheless, the scattered intensity  $I$  changes rapidly with the wavenumber  $q$  near a peak. This allows us to use the derivative,  $d(\log_{10} I)/dq$ , to locate the lower and the upper bounds of the peak, which are, respectively, associated with the local maximum and minimum, as illustrated by the shadowed regions in Figure 2b. A similar analysis is performed for all polymers (Figure S4), and the upper and lower bounds of the primary peak are listed in Table 1. The average

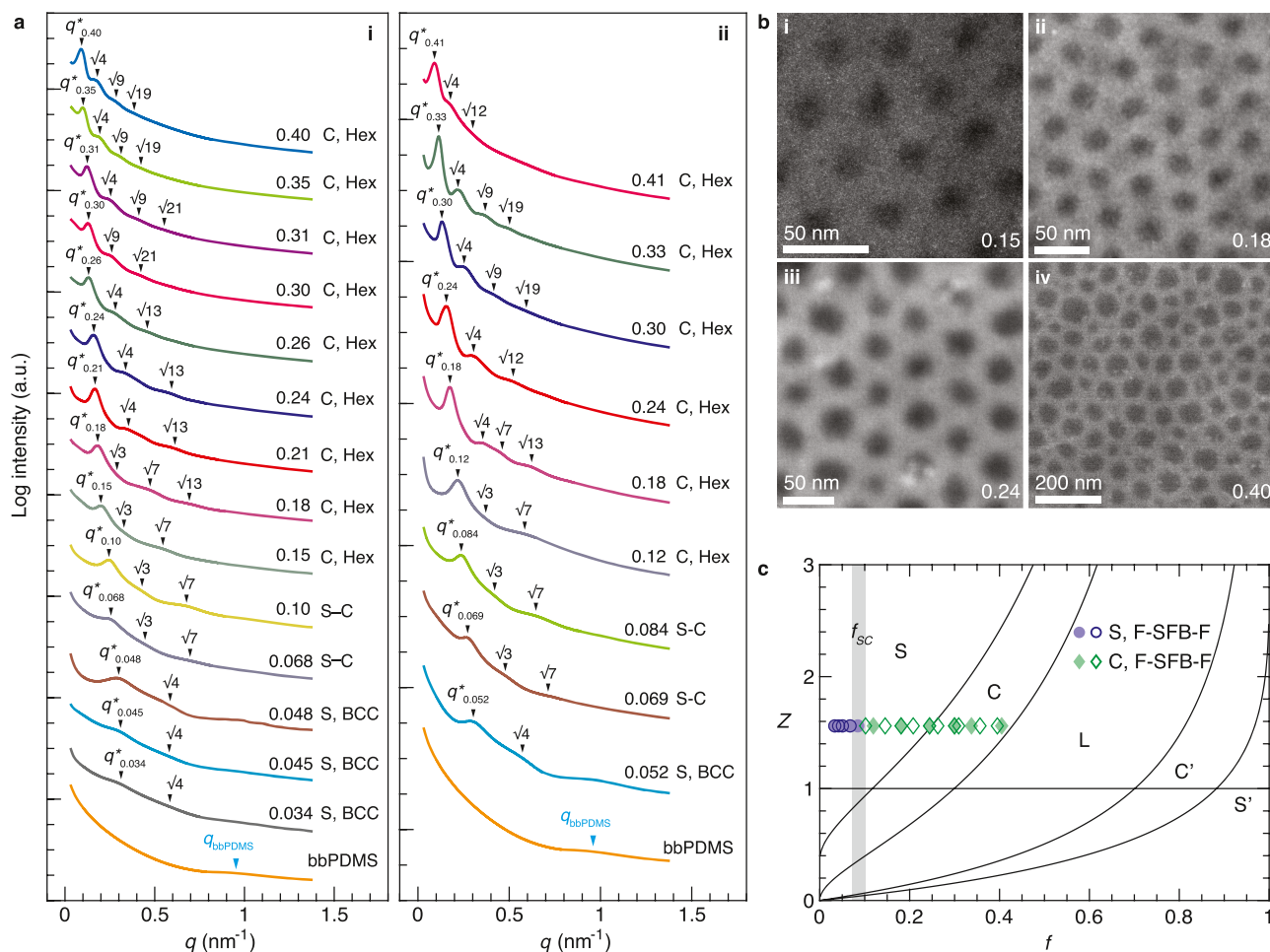


**Figure 2.** SAXS and TEM determine the type of self-assembled microstructure. (a) 2D SAXS pattern of sample  $S_{13}$  with  $f = 0.35$  (Table 1). (b) (i) Radially averaged 1D scattering intensity  $I$  as a function of the magnitude of wavevector  $q$ . (ii) The dependence of derivative  $d(\log_{10} I)/dq$  on  $q$ . The solid red line is the spline fit to the data as the guidance for the eye. (c) A representative dark-field TEM image of a film with the thickness of 200 nm sliced using a microtome. The bright dots on the lower left are randomly deposited gold nanoparticles as fiducial markers for the image alignment for electron tomography (Movie S1).

wavenumber,  $q_n$ , of the  $n$ th peak corresponds to the deflection point between the lower bound and the upper bound, as denoted by the dashed lines in Figure 2b.

We attempt to determine the type of microstructure by comparing the positions of the characteristic peaks to the allowed reflections for a space group using ratios of  $q/q^*$ , where  $q^*$  is the wavenumber of the primary scattering peak at the lowest wavenumber.<sup>33</sup> For example, the sample with  $f = 0.35$  exhibits a relation  $q/q^* = 1.0, 2.0 \pm 0.2, 3.1 \pm 0.2, \text{ and } 4.3 \pm 0.3$  (Figure 2b(i)). Within the measurement error, unfortunately, this relation can be associated with either a hexagonal lattice of cylinder morphology or a periodic 1D structure of lamellae morphology (see the Supporting Information text). Consequently, because of relatively broad higher-order peaks, the relation  $q/q^*$  alone is insufficient for precisely determining the type of microstructure.

To complement SAXS measurements, we use TEM to directly visualize the morphology of the self-assembled polymers. For the polymer with  $f = 0.35$ , we use a microtome to slice the same bulk polymer as used for SAXS to obtain a thin film with a thickness of 200 nm (Experimental Section). Instead of using conventional bright-field TEM, we developed a technique based on dark-field TEM that uses diffracted rather than transmitted beam to image microdomains; this allows a sharp contrast of different domains without staining (Experimental Section). The observed 2D morphology exhibits a hexagonal pattern (Figure 2c), which is further confirmed by the three-dimensional (3D) microstructure rendered from electron tomography (Movie S1). Collectively, these results demonstrate that the LBBL polymer with  $f = 0.35$  forms a cylinder rather than a lamellar microstructure. Importantly, these results demonstrate that the combination of SAXS and TEM allows for the unambiguous determination of the type of microstructure.

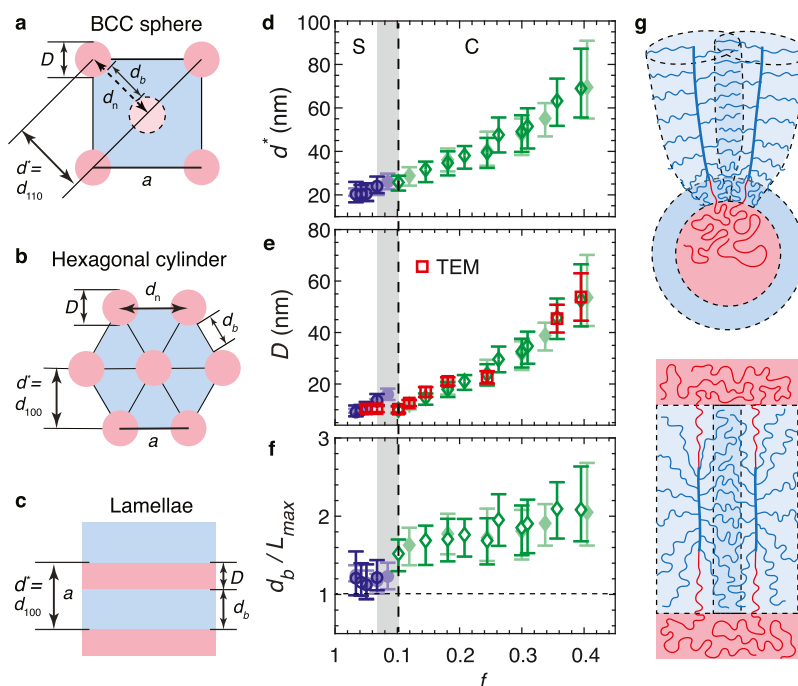


**Figure 3.** SFB widens the regime for the cylinder morphology. (a) Radially averaged 1D scattering intensity  $I$  as a function of  $q$ : (i) polymers with the same bottlebrush middle block (batch 1, Table 1); (ii) polymers with the bottlebrush middle block synthesized from different batches (batches 2–5, Table 1 and Figure S8). The assignment of peak relations is based on the peak analysis described in Figure 2 and listed in Figure S4. As  $f$  increases, the primary scattering peak,  $q^*$ , shifts to smaller wavenumbers associated with larger characteristic length scales. The melt of bottlebrush PDMS exhibits a characteristic peak at  $q_{\text{bbPDMS}} = 0.964 \text{ nm}^{-1}$ . The associated length scale,  $2\pi/q_{\text{bbPDMS}} = 6.5 \text{ nm}$ , corresponds to the distance between the backbone of two neighboring bottlebrush molecules. This value is smaller than twice the size of the side chain, 11.6 nm, suggesting interdigitated side chains between neighboring bottlebrush molecules, as illustrated in Figure 4g. (b) Representative dark-field TEM images of the self-assembled microstructures. Dark regions are domains formed by end linear PBnMA blocks, and white regions are bottlebrush PDMS domains. (c) A two-parameter ( $Z$ ,  $f$ ) phase diagram predicted by a recent SCFT study for the self-assembly of strongly segregated bottlebrush-based AB-type BCPs (reprinted in part with permission from ref 20; copyright 2020 American Chemical Society).  $Z$  is determined by the difference in the molecular architecture between the A and B blocks:  $Z \equiv \beta(l_A b_A / v_A)^{1/2} (l_B b_B / v_B)^{1/4}$ . Here,  $l$  and  $v$  are, respectively, the size and the volume of a chemical monomer,  $b$  is the length of a Kuhn segment,  $n$  is the number of chemical monomers per side chain, and  $\beta$  is a numerical factor on the order of unity; the subscripts A and B, respectively, refer to the end linear chemical and the side chains of the bottlebrush. In the theoretical study, a  $Z$  value equal to 1.6 is used for the bottlebrush with the same chemistry and molecular architecture as in this current study. Solid lines are predicted boundaries between different types of microstructures: S and S'—sphere; C and C'—cylinder; and L—lamellae. Empty blue and green symbols are experimental data obtained from F-SFB-F polymers with the bottlebrush synthesized from the same batch, and the filled symbols are those with the bottlebrush synthesized from different batches. Circles: BCC packing of spheres; diamonds: hexagonal lattice of cylinders. The shadowed region indicates the crossover between the sphere and cylinder phases.

**Phase Diagram.** Using a combination of SAXS and TEM, we determine the crossover volume fractions between different phases (Figure 3). At relatively small volume fractions,  $0.07 \leq f \leq 0.10$ , the diffraction peaks exhibit relative positions,  $q/q^* = \sqrt{1}, \sqrt{3}, \sqrt{7}$ , suggesting a hexagonal lattice of the cylinder (Figure 3a). However, dark-field TEM images do not exhibit an obvious hexagonal pattern (Figure S5a,b); this is likely because of relatively small domain sizes and weak contrast associated with low volume fractions of end blocks. Yet, at a slightly higher volume fraction,  $f = 0.12$ , TEM reveals a hexagonal cylinder morphology (Figure S5c). Such an

ordering becomes more obvious and is of long range for  $f = 0.15$  [Figure 3b(i)]. Therefore, the crossover volume fraction between the sphere and cylinder phases is likely within  $0.70 \leq f_{\text{SC}}^{\text{SFB}} \leq 0.10$ .

Interestingly, even at a high volume fraction,  $f = 0.40$ , the microstructure remains to be a cylinder, as clearly shown by the TEM image in Figure 3b(iv) and large-area view in Figure S5d. Determining the crossover volume fraction between the cylinder and lamellae requires the controlled synthesis of high-quality samples with  $f > 0.40$  or polymers with the number of repeating units  $> 1200$ . This represents a challenge for ATRP and will be the subject of a future study. Nevertheless, these



**Figure 4.** Architectural SFB rearranges its linear side chains to form remarkably large domains. (a–c) Illustrations of characteristic lengths for BCC packing of spheres, hexagonal lattice of cylinders, and lamellar microstructure.  $d^*$  corresponds to the first permitted Bragg peak of a microstructure,  $a$  is the lattice constant,  $D$  is the size of the domain formed by end PBnMA blocks,  $d_b$  is the distance bridging two nearest-neighbor PBnMA domains, and  $d_n$  is the distance between the center of two nearest-neighbor PBnMA domains. For BCC,  $a = \sqrt{2} d_{110} = \sqrt{2} d^*$ ; for hexagonal cylinder,  $a = (2/\sqrt{3})d_{100} = (2/\sqrt{3})d^*$ ; and for lamellae,  $d^* = d_{100} = a$ . (d–f) Dependencies of the primary characteristic length  $d^*$ , PBnMA domain size  $D$ , and normalized bridging distance  $d_b/L_{\max}$  on the volume fraction  $f$  of end blocks. Empty symbols are data for F-SFB-F polymers with the same batch of the bottlebrush middle block, and the filled symbols are for polymers with different batches of the bottlebrush middle block. Red squares are the diameters of the end block domains directly measured from TEM (Figure S6). (g) Illustration for the molecular picture of the anomalous self-assembly of F-SFB-F triblock copolymers in spherical, hexagonal cylinder, and lamellar microstructures. The end linear blocks are pulled out to generate additional space for the long side chains, alleviating packing frustration near curved interfaces and effectively increasing the size of the bottlebrush domain.

results show that the cylinder morphology continues at volume fractions no less than 0.40. The window for the cylinder phase,  $f_C^{\text{SFB}} \in (0.10, >0.40)$ , is much wider than that of strongly segregated linear flexible diblock and triblock copolymers,  $f_C^{\text{F}} \in (0.14, 0.35)$ .<sup>34</sup>

Surprisingly, our experimental findings contradict recent SCFT theoretical predictions for bottlebrush-based BCPs.<sup>20</sup> The theoretical study uses bottlebrush polymers with the same chemistry and molecular architecture as in our current study. This allows us to apply the theory directly to the F-SFB-F triblock polymers without introducing any additional assumptions. The predicted window for the cylinder phase,  $f_C^{\text{SCFT}} \in (0.22, 0.45)$ , starts at the volume fraction much higher than our experimental findings, as shown by the colored symbols in Figure 3c. Such a large discrepancy indicates that the existing SCFT calculation cannot explain our experimental findings.

The phase behavior for F-SFB-F triblock copolymers is dramatically different from that of semiflexible linear BCPs. Existing experimental studies for linear flexible–semiflexible–flexible (F-SF-F) triblock copolymers<sup>35</sup> reveal either a disordered phase or an ordered lamellar microstructure. Consistent with these experimental findings, SCFT calculations suggest that linear flexible–semiflexible (F-SF) diblock copolymers<sup>36,37</sup> are prone to form highly ordered lamellar microstructures, except in the 2D space where nonlamellar microstructures become possible.<sup>38</sup> By contrast, F-SFB-F triblock copolymers exhibit both spherical and cylindrical

microstructures. Compared to linear F-SF-F triblock copolymers, which transition from the cylinder to lamellar morphology with  $f$  above 0.20,<sup>35</sup> F-SFB-F triblock copolymers remain to be a cylinder up to at least 0.40. These differences suggest that the self-assembly of architecturally semiflexible BCPs is both qualitatively and quantitatively different from that of simple linear semiflexible–flexible BCPs.

**Anomalous Characteristic Length Scales.** The difference between architecturally semiflexible and simple linear BCPs is further highlighted by the characteristic lengths of the microstructures. Based on the magnitude of the primary scattering wavevector  $q^*$ , we obtain the length scale,  $d^* = 2\pi/q^*$ , which corresponds to the first permitted Bragg peak of a microstructure, as, respectively, illustrated for the BCC sphere, hexagonal cylinder, and lamellar phase in Figure 4a–c. As the microstructure transitions from sphere to cylinder,  $d^*$  increases dramatically from 20 to 70 nm. The relatively large  $d^* \approx 70 \pm 20$  nm for the cylinder structure is consistent with the light blue color of the polymer (Figure 1e).

To quantify the contribution of end blocks to characteristic lengths, we calculate the size of the domain formed by the end blocks,  $D$ , based on two experimentally measured parameters: the volume fraction  $f$  and the length  $d^*$ . For a BCC packing of spheres,  $D = (3/\pi)^{1/3} f^{1/3} a$ , in which the lattice constant  $a = \sqrt{2} d^*$  (Figure 4a); for a hexagonal lattice of cylinders,  $D = (6/\sqrt{3}\pi)^{1/2} f^{1/2} a$ , in which  $a = (2/\sqrt{3})d^*$  (Figure 4b); for a 1D packing of lamellae,  $D = fa = fd^*$  (Figure 4c). As

expected, for each microstructure,  $D$  increases with  $f$  or the MW of the end blocks (Figure 4e). Moreover, the calculated values of  $D$  based on SAXS measurements agree with that directly measured from TEM, as shown by red squares in Figure 4e and histograms in Figure S6. In addition, the volume fraction  $f$  determined by NMR is consistent with that calculated from TEM, as shown by histograms in Figure S7 and Table S1. These results confirm the classification of the type of microstructure self-assembled by F-SFB-F triblock copolymers (Figure 3).

To quantify the size of the bottlebrush domain, we define  $d_b$  as the distance bridging two nearest-neighbor PBNMA domains, as illustrated for different types of microstructures in Figure 4a–c. Specifically, for a BCC packing of spheres,  $d_b = \sqrt{3}a/2 - D$  and  $a = \sqrt{2}d^*$ ; for a hexagonal lattice of cylinders,  $d_b = a - D$  and  $a = (2/\sqrt{3})d^*$ ; and for a 1D packing of lamellae,  $d_b = a - D$  and  $a = d^*$ . Furthermore, we introduce a parameter,  $d_b/\mathcal{L}_{\max}$ , that is defined as the ratio of the bridging distance to the contour length of the bottlebrush backbone; this parameter describes the extent to which the bottlebrush is stretched.

Remarkably, the value of  $d_b/\mathcal{L}_{\max}$  is abnormally large regardless of the type of microstructures. Specifically,  $d_b/\mathcal{L}_{\max}$  is about 1.2 in the sphere phase (blue symbols in Figure 4f); this is consistent with that accidentally observed in our previous study, in which experiments were designed for studying the effects of bottlebrush flexibility on the self-assembly of LBBF triblock copolymers.<sup>45</sup> Moreover, in the cylinder phase,  $d_b/\mathcal{L}_{\max}$  increases from 1.4 to nearly 2 as  $f$  increases from 0.10 to 0.35 and stays around this value at higher  $f$  (Figure 4f). This is extremely surprising because  $\mathcal{L}_{\max}$  is the maximum to which the bottlebrush backbone can be stretched. Thus, it is expected that  $d_b/\mathcal{L}_{\max}$  must not be larger than 1. This upper limit has been proven not only for all kinds of simple linear BCPs regardless of their flexibility but also for bottlebrush diblock<sup>39</sup> and triblock<sup>40</sup> copolymers with all the blocks of the same diameter. Although polydisperse diblock copolymers with a PDI of about 2 can have large domain distances,<sup>41–43</sup> in our study, the bottlebrush polymer is of relatively narrow dispersity with a PDI of 1.15. Moreover, all triblock copolymers have the same bottlebrush middle block. These preclude the polymer dispersity from being the cause of the unexpectedly large bridging distance. Nevertheless, to confirm our counterintuitive findings, we synthesize an additional series of F-SFB-F triblock copolymers with  $f$  up to 0.41. Instead of using the same SFB for all triblock copolymers, we synthesize multiple batches of bottlebrush polymers that have the same average number of side chains but slightly different dispersities (Figure S8 and Table 1). Results from independent experiments are consistent with each other, as shown by the SAXS measurements [Figure 3a(ii)], the phase diagram (filled symbols in Figure 3c), and the characteristic length scales (filled symbols in Figure 4d–f). These results demonstrate that the observed large bridging distance is valid and reproducible.

We propose a molecular mechanism to explain the anomalous assembly of F-SFB-F ABA triblock copolymers. In the self-assembled microstructure, the interfacial repulsion between the highly incompatible A and B microdomains generates tension along the polymer backbone. Compared to a classical linear polymer, the cross section of a SFB is much larger, resulting in a much larger interfacial area per triblock

copolymer. Consequently, the resulted interfacial repulsion may be large enough to pull out a part of the linear chain from the A domain. This effectively increases the size of the bottlebrush domain or the bridging distance, as illustrated in Figure 4g.

Conceptually, the proposed molecular picture can be rationalized in the context of free-energy minimization. We consider the total free energy,  $F_t$ , of a single F-SFB-F triblock copolymer. It consists of two components:  $F_t = F_{\text{int}} + F_{\text{ent}}$  in which  $F_{\text{int}}$  is the interfacial free energy that is proportional to the total interfacial area  $A_t$  and  $F_{\text{ent}}$  is the configurational entropy of polymer chains. The interfacial area consists of two parts:  $A_t = A_l + A_c$  in which  $A_l$  is determined by the “invaded” linear segment that is pulled into the bottlebrush domain and  $A_c$  is determined by the area of contact between the bottlebrush and the domain formed by the end blocks. As the size of the “invaded” segment increases,  $A_l$  increases; by contrast,  $A_c$  must decrease to conserve the bottlebrush volume. Therefore, there must be an optimized size for the “invaded” linear segment to minimize the interfacial free energy.

Similarly, the entropic free energy consists of two parts:  $F_{\text{ent}} = F_{\text{bb}} + F_{\text{sc}}$  in which  $F_{\text{bb}}$  and  $F_{\text{sc}}$  are, respectively, the configurational entropy of the triblock polymer backbone and the side chains in the bottlebrush. Because of strong steric repulsion among the overlapping side chains, the backbone of the SFB is already prestretched to its contour length before the microphase separation. Therefore,  $F_{\text{bb}}$  is dominated by the “invaded” linear section and increases with the section size. By contrast, as the size of the “invaded” section increases, it generates more space near the two ends of the bottlebrush for the densely grafted side chains to occupy; this results in less steric repulsion among the side chains and thus the decrease of  $F_{\text{sc}}$ . Thus, there must be an optimized size for the “invaded” linear section to minimize the entropic free energy.

Quantitatively, the concept of the “invaded” linear polymer section permits the remarkably large length scales in the self-assembled microstructures. For instance, the contour length of a PDMS side chain is about 20 nm, much larger than the length,  $\sim 7$  nm, required for the largest bridging distance at high volume fractions, as shown by the green diamonds on the right in Figure 4f. Moreover, the “invaded” linear section provides additional space for the densely grafted side chains to rearrange to alleviate packing frustration, which becomes exacerbated near highly curved interfaces for the spherical and cylindrical phases, as illustrated in Figure 4g. This molecular picture is qualitatively different from the one proposed for spherical microstructure self-assembled by LBBF triblock copolymers, in which the side chains near the ends of the bottlebrush are stretched along the backbone in the direction away from and perpendicular to the highly curved interface.<sup>44</sup> Taken together, the concept of “invaded” linear section not only allows for the minimization of free energy but also avoids packing frustration, which are the two governing mechanisms for the self-assembly of BCPs.<sup>45</sup>

## CONCLUSIONS

We have systematically investigated the self-assembly of strongly segregated linear–semiflexible bottlebrush–linear triblock copolymers. We discover that the window for the cylinder morphology,  $f_C^{\text{SFB}} \in (0.10, >0.41)$ , is much wider than that for flexible linear ABA triblock copolymers,  $f_C^{\text{F}} \in (0.14, 0.35)$ , and that predicted by recent SCFT calculations,  $f_C^{\text{SCFT}} \in (0.22, 0.45)$ , for bottlebrush BCPs of the same chemistry and

molecular architecture.<sup>20</sup> Remarkably, regardless of the type of microstructure, the size of the bottlebrush domain  $d_b$  is always larger than the contour length  $\mathcal{L}_{\max}$  of the bottlebrush backbone. Even more surprisingly, the ratio between the two length scales,  $d_b/\mathcal{L}_{\max}$ , becomes extremely large around 2 at high volume fractions; this observation is reproducible and further supported by the structural color of the self-assembled polymers. This anomalous self-assembly is likely because that a part of the linear end blocks is pulled into the bottlebrush domain, which effectively increases the bottlebrush domain size. The concept of such “invaded” linear end blocks is qualitatively different from the classical understanding of ABA triblock copolymers, where the bridging distance between two neighboring A domains can never be larger than the contour length of the middle B block. The observed anomalous self-assembly of architecturally semiflexible BCPs calls for further theoretical studies. It also cautions the use of the conventional definition of the bottlebrush contour length as that of the bottlebrush backbone,<sup>10,16,13,46</sup> which often ignores the contribution of side chains. The side chains can rearrange to occupy the space near the ends of the bottlebrush backbone. This effectively increases the bottlebrush contour length, and such an increase becomes significant for SFB polymers with long side chains. Nevertheless, our experimental findings reveal previously unrecognized mechanisms for the self-assembly of architecturally complex BCPs. This knowledge may inform the design of multifunctional microstructures with an exceptional combination of long-range ordering and large characteristic length scales.

## EXPERIMENTAL SECTION

**Materials.** MCR-M17, monomethacryloxypropyl-terminated PDMS, average molar mass 5000 g/mol, was purchased from Gelest and purified using basic aluminum oxide columns to remove inhibitors before use. Benzyl methacrylate (96%) was purchased from Sigma-Aldrich and purified using basic aluminum oxide columns to remove inhibitors before use. Copper(II)chloride ( $\text{CuCl}_2$ , 99.999%), *tris*[2-(dimethylamino)ethyl]amine ( $\text{Me}_6\text{TREN}$ ), ethylene bis(2-bromoisobutyrate) (2f-BiB, 97%), tin(II) 2-ethylhexanoate [ $\text{Sn}(\text{EH})_2$ , 92.5–100%], anisole ( $\geq 99.7\%$ ), and *p*-xylene ( $\geq 99.7\%$ ) were purchased from Sigma-Aldrich and used as received. Methanol (Certified ACS), diethyl ether (Certified ACS), dimethylformamide (DMF, Certified ACS), tetrahydrofuran (THF, Certified ACS), and THF [high-performance liquid chromatography (HPLC)] were purchased from Fisher and used as received.

**Polymer Synthesis and Characterization.** To synthesize a F-SFB-F triblock copolymer, we first synthesize the middle bottlebrush block and then use the bottlebrush as a macroinitiator to grow the end linear blocks (Figure S1). Here, we describe the detailed synthesis protocol using the F-SFB-F polymer with the highest volume fraction as an example.

**Step I. Synthesis of Bottlebrush PDMS.** A 100 mL Schlenk flask is charged with 2f-BiB (7.2 mg, 0.02 mmol), MCR-M17 (30 g, 6 mmol), *p*-xylene (10 mL), and anisole (10 mL). We dissolve  $\text{Me}_6\text{TREN}$  (46 mg, 0.2 mmol) and  $\text{CuCl}_2$  (2.7 mg, 0.02 mmol) in 1 mL of DMF to make a catalyst solution. Then, we add 120  $\mu\text{L}$  of catalyst solution, containing  $2.4 \times 10^{-2}$  mmol  $\text{Me}_6\text{TREN}$  and  $2.4 \times 10^{-3}$  mmol  $\text{CuCl}_2$ , to the mixture and bubble it with nitrogen for 60 min to remove oxygen. Afterward, the reducing agent,  $\text{Sn}(\text{EH})_2$  (38.9 mg, 0.096 mmol) in 200  $\mu\text{L}$  of *p*-xylene, is quickly added to the reaction mixture using a glass syringe. We seal the flask and then immerse it in an oil bath at 60 °C to start the reaction. We stop the reaction after 205 min and take a small amount of the mixture to determine the conversion using proton NMR (see Supporting Information, NMR spectra) and GPC (Figure S3). These are two methods that allow the independent measurement of the conversion, and both give the same value of 17%.

This results in a bottlebrush polymer with the degree of polymerization of 51, corresponding to the number-average MW of 255 kg/mol.

The remaining reaction mixture is diluted with THF and passed through a neutral aluminum oxide column to remove the catalyst. The collected solution is concentrated by a rotary evaporator (Buchi R-205). To separate the bottlebrush polymer from the unreacted macromonomers, we create a co-solvent, a mixture of methanol and diethyl ether with a volume ratio of 3:2, which is a good solvent for the macromonomers but not for the bottlebrush PDMS. After precipitation, we further centrifuge the mixture to separate the polymer from the solvent and re-dissolve the separated polymer in THF to make a homogeneous solution. We repeat this precipitation procedure seven times to ensure that all unreacted macromonomers and impurities are completely removed. We use GPC to measure the PDI of the final product, which is 1.15 for this bbPDMS (Figure 1c). At room temperature, bbPDMS is a viscous, transparent liquid.

**Step II. Synthesis of LBBL Triblock Copolymers.** A 25 mL Schlenk flask is charged with BnMA (893 mg, 5.07 mmol), macroinitiator (bbPDMS, 255 kg/mol, 255 mg,  $1 \times 10^{-3}$  mmol), *p*-xylene (2.6 mL), and anisole (1.3 mL). We dissolve  $\text{Me}_6\text{TREN}$  (46 mg, 0.2 mmol) and  $\text{CuCl}_2$  (2.7 mg, 0.02 mmol) in 1 mL of DMF to make a catalyst solution. We add 85  $\mu\text{L}$  of catalyst solution, containing  $1.7 \times 10^{-2}$  mmol  $\text{Me}_6\text{TREN}$  and  $1.7 \times 10^{-3}$  mmol  $\text{CuCl}_2$ , to the mixture and bubble it with nitrogen for 45 min to remove oxygen. Afterward, the reducing agent,  $\text{Sn}(\text{EH})_2$  (27.5 mg,  $6.8 \times 10^{-2}$  mmol) in 200  $\mu\text{L}$  of *p*-xylene, is quickly added to the reaction mixture using a glass syringe. Then, we seal the flask and immerse it in an oil bath at 60 °C. The reaction is stopped after 360 min. The reaction mixture is diluted in THF and passed through a neutral aluminum oxide column to remove the catalyst, and the collected solution is concentrated by a rotavapor. Instead of using a methanol-diethyl ether co-solvent as in Step I, we create a co-solvent, a mixture of methanol and acetone with a volume ratio of 1:1 for precipitation for three times; this completely removes all unreacted monomers and almost all free PBnMA due to the chain-transfer reaction during ATRP. After purification, the sample is dried in a vacuum oven (Thermo Fisher, Model 6258) at room temperature for 24 h. A small amount of the polymer is used for  $^1\text{H}$  NMR analysis and GPC analysis. From  $^1\text{H}$  NMR analysis, the degree of polymerization of BnMA is 1140, corresponding to a MW 100.4 kg/mol for each of the two end blocks. From GPC analysis, the PDI is 1.71 for this triblock copolymer (Figure 1c). At room temperature, the polymer is a semitransparent, blue, stiff solid.

**$^1\text{H}$  NMR Characterization.** We use  $^1\text{H}$  NMR to determine the number of side chains per bottlebrush and the volume fraction of PBnMA. The former one is calculated based on the conversion of PDMS macromonomers into bottlebrush PDMS, which is measured by the NMR spectra of the raw reaction mixture, as documented in a previous publication.<sup>45</sup> The volume fraction of PBnMA is determined based on the NMR spectra of purified triblock copolymers (see Supporting Information, NMR spectra).

**GPC Characterization.** GPC measurements are performed using a TOSOH EcoSEC HLC-8320 GPC system with two TOSOH Bioscience TSKgel GMH<sub>HR</sub>-M 5  $\mu\text{m}$  columns in series and a refractive index detector at 40 °C. HPLC grade THF is used as the eluent with a flow rate of 1 mL/min. The samples are dissolved in THF with a concentration of around 5 mg/mL. The GPC data of all bbPDMS polymers and the corresponding LBBL polymers are shown in Figures 1c and S8. The MW and PDI of all samples are summarized in Table 1.

**SAXS/WAXS Measurements.** To prepare a sample for SAXS/WAXS characterization, we dissolve a triblock copolymer in toluene at a concentration of 100 mg/mL with a total volume of 3 mL in a glass vial and allow the solvent to slowly evaporate for 24 h. Because toluene is a solvent close to be equally good for PBnMA and PDMS, it avoids the effects of solvent selectivity on the self-assembly. After being further thermally annealed for 6 h in a vacuum oven at 180 °C and then slowly cooled down at a rate of 0.5 °C/min to room temperature, the structures of the samples do not change. For each sample, we use a relatively large amount of polymer to obtain a bulk



material with the smallest dimension larger than 1 mm, more than  $10^4$  times the size of a triblock copolymer; this prevents the substrate or boundary effects on the self-assembly process.

We use the Soft Matter Interfaces (12-ID) beamline<sup>47</sup> at the Brookhaven National Laboratory to perform SAXS/WAXS measurements on annealed bulk polymers. The sample-to-detector distance is 8.3 m, and the radiation wavelength is  $\lambda_x = 0.77 \text{ \AA}$ . The scattered X-rays are recorded using an in-vacuum Pilatus 1 M detector, consisting of 0.172 mm square pixels in a  $941 \times 1043$  array. The raw SAXS images are converted into  $q$ -space, visualized in Xi-CAM software,<sup>48</sup> and radially integrated using a custom Python code. The 1D intensity profile,  $I(q)$ , is plotted as a function of the scattering wavevector,  $|q| = q = 4\pi\lambda_x^{-1}\sin(\theta/2)$ , where  $\theta$  is the scattering angle.

**Transmission Electron Microscopy.** We use a combination of pressurized solvent vapor and thermal annealing to prepare samples for TEM imaging. We build a glass chamber with a sample stage, on which is placed a carbon film-coated copper TEM grid. Moreover, the bottom of the glass chamber is filled with toluene. In parallel, we prepare a F-SFB-F polymer solution by dissolving the polymer in toluene with a concentration of 5 mg/mL. The polymer solution is passed through a syringe filter with a pore size of  $0.45 \mu\text{m}$  to remove possible dusts. We add  $7 \mu\text{L}$  of polymer solution to the TEM grid, seal the glass chamber immediately, transfer the chamber into an oven with temperature of  $100 \text{ }^\circ\text{C}$ , and maintain the temperature for 24 h. This generates a toluene vapor pressure of 75 kPa. Afterward, the oven is slowly cooled down at a rate of  $0.5 \text{ }^\circ\text{C}/\text{min}$  to room temperature. Further increasing the annealing time to 3 days does not change the morphology of the polymers.

We use a hollow-cone dark-field transmission electron microscope (FEI Titan) at the electron energy of 300 keV with a tilt angle of  $0.805^\circ$  to characterize the annealed samples. This tilt angle allows for a sharp contrast between PDMS and PBnMA domains without staining. The size of spherical domains is calculated using ImageJ, and more than 200 domains are used to ensure sufficient statistics.

**Electron Tomography.** We use a microtome to slice the polymer for electron tomography. To prepare the sample for the microtome, we mount a piece of annealed bulked polymer on a “dummy” block using a two-part adhesive epoxy glue (Epoxy MS-907 Plus, Miller-Stephenson). The glue is left to cure for 24 h at room temperature. Using a Reichert Leica Ultracut S Microtome (Leica Microsystems, Vienna, Austria) equipped with a diamond knife, we slice the sample to a serial of sections with 200 nm thickness each and collect the sections on formvar-coated copper slot grids. Colloidal gold nanoparticles (15 nm; Sigma-Aldrich) are deposited to both sides of the sections collected on copper slot grids to serve as fiducial markers for subsequent image alignment.

For single-axis electron tomography, a series of tilted views are recorded using a F20 electron microscope (Thermo-Fisher, formerly FEI) operating at 200 kV. Images are captured every  $1^\circ$  over a  $\pm 60^\circ$  range and a pixel size of 0.3731 or 0.7439 nm using a Tietz TVIPS XF416 camera ( $4k \times 4k$ ). We use the IMOD software package (<http://bio3d.colourado.edu/imod>) that contains all the programs needed for calculating electron tomograms.<sup>49</sup> For image processing, the tilted views are aligned using the positions of the colloidal gold particles as fiducial markers. Tomograms are computed using the R-weighted back-projection algorithm.<sup>50</sup>

## ■ ASSOCIATED CONTENT

### SI Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.macromol.1c01911>.

Discussion on characteristic SAXS peaks for different types of microstructures, GPC traces of all bbPDMS and LBBL polymers,  $^1\text{H}$  NMR spectra of selected bbPDMS and all LBBL polymers, determination of characteristic peaks of SAXS measurements, example TEM images of LBBL polymers, and domain diameters and distances of LBBL polymers (PDF)

Electron tomography measurement for the LBBL polymer with  $f = 0.35$  (AVI)

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### Author Contributions

L.H.C. conceived the study. L.H.C. and S.N. designed the research. S.N. and L.H.C. performed the research. S.R. performed TEM tomography characterization. S.N. and L.H.C. analyzed data. F.Z. helped with polymer synthesis. G.F. and M.Z. helped with SAXS/WAXS measurements and data analysis. L.H.C. and S.N. wrote the paper. All authors reviewed and commented on the paper. L.H.C. supervised the research.

### Notes

The authors declare no competing financial interest.

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